

Calculator

2011 #1.

For  $0 \leq t \leq 6$ , a particle is moving along the x-axis. The particle's position,  $x(t)$ , is not explicitly given. The velocity of the particle is given by  $v(t) = 2\sin(e^{t^4}) + 1$ .

- a. Find the total distance traveled by the particle from  $0 \leq t \leq 6$ .

$$\int_0^6 |v(t)| dt = 12.573$$

77. Water is pumped out of a lake at the rate  $R(t) = 12\sqrt{\frac{t}{t+1}}$  cubic meters per minute, where  $t$  is measured in minutes. How much water is pumped from time  $t = 0$  to  $t = 5$ ?

- A) 9.439 cubic meters  
 B) 10.954 cubic meters  
 C) 43.816 cubic meters  
 D) 47.093 cubic meters  
 E) 54.772 cubic meters

$$\int_0^5 R(t) dt =$$

87. An object traveling in a straight line has position  $x(t)$  at time  $t \geq 0$ . If the initial position is  $x(0) = 2$  and the velocity of the object is  $v(t) = \sqrt[3]{1+t^2}$ , what is the position of the object at time  $t = 3$ ?

- A) .431    B) 2.154    C) 4.512    D) 6.512    E) 17.408

$$2 + \int_0^3 v(t) dt =$$

~~$$\int (1+t^2)^{1/3} dt$$~~

What you'll Learn About

- Finding the area between 2 curves

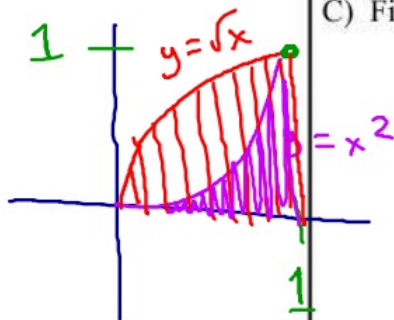
A) Find the area between the curve  $y = \sqrt{x}$  and the x-axis from  $[0, 1]$ .

$$A = \int_0^1 x^{1/2} dx = \left. \frac{2}{3} x^{3/2} \right|_0^1 = \frac{2}{3}$$

B) Find the area between the curve  $y = x^2$  and the x-axis from  $[0, 1]$ .

$$A = \int_0^1 x^2 dx = \left. \frac{1}{3} x^3 \right|_0^1 = \frac{1}{3}$$

C) Find the area between the curves  $y = x^2$  and  $y = \sqrt{x}$



$$A = \int_0^1 \sqrt{x} dx - \int_0^1 x^2 dx$$

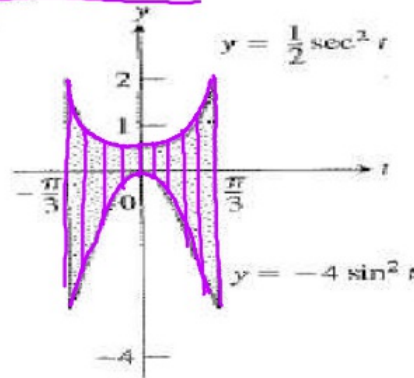
Top Curve - Bottom Curve

$$A = \int_0^1 (\sqrt{x} - x^2) dx = \frac{1}{3}$$

~~$$A = \int_0^1 |(x^{1/2} - x^2)| dx = \frac{1}{3}$$~~

Using your calculator find the area of the shaded region.

2.



$$A = \int_{-\pi/3}^{\pi/3} \left[ \frac{1}{2} \sec^2 t - (-4 \sin^2 t) \right] dt$$

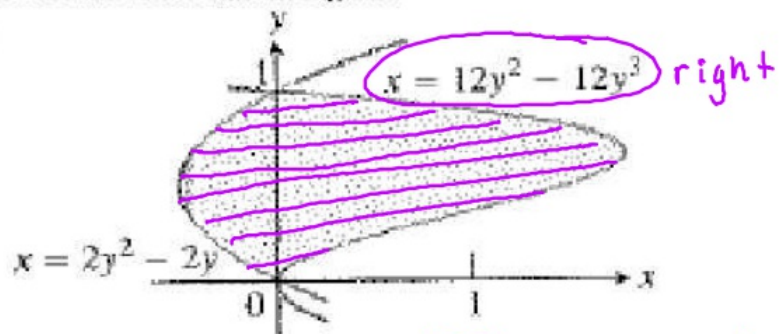
$$A = 4.188$$

Top-Bottom  
equations  $y =$   
everything  $x$

Equations  
solved for  $x$   
Right-Left +  
everything  $y$

Find the area of the shaded region.

4.



$$A = \int_0^1 \left[ (12y^2 - 12y^3) - (2y^2 - 2y) \right] dy$$

$$A = \int_0^1 (10y^2 - 12y^3 + 2y) dy$$

$$A = \left[ \frac{10}{3} y^3 - 3y^4 + y^2 \right]_0^1 = \frac{10}{3} - 3 + 1 = \frac{4}{3}$$